# CHAPTER 11

# THE ACQUISITION OF FUNCTIONAL PLANNING AND PROGRAMMING KNOWLEDGE: DIAGNOSIS, MODELING, AND USER-ADAPTED HELP[1]

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## ABSTRACT

A three-level approach to model processes of problem solving and the acquisition and optimization of knowledge was developed. First, a general theoretical framework describes problem solving phases, impasse driven knowledge acquisition, and success driven knowledge optimization. Second, a State Model of hypothetical intermediate knowledge states may be used for online diagnoses of learner's domain knowledge and for generating learner-adapted help and information. Third, a Process Model closes the gap between the theoretical framework and the State Model. The approach enables a variety of empirical predictions about problem solving actions, action and time constraints, and effects of help information. In addition, it has implications for the design of intelligent knowledge communication systems. The ABSYNT Problem Solving Monitor (PSM) was developed in line with these design requirements. It supports learner's acquisition of basic programming concepts while working in a visual, functional programming language. The learner may test hypotheses about solution proposals, plans and intentions, and incomplete plan fragments. Thus help is supplied at impasses, the use of preknowledge is encouraged, and different problem solving phases are supported. In addition, a State Model is designed to supply help adapted to the current knowledge state of the learner.

The development of executable models of human information processing and their empirical validation has become an important research area, especially

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233

concerning processes of knowledge acquisition. Since models of this kind explicitly represent hypothetical knowledge structures and processes, they enable detailed hypotheses concerning the representation and change of knowledge, and they enable detailed and sometimes surprising predictions. Thus, they contribute to psychological theorizing and to basic research. On the other hand, modeling the acquisition and change of knowledge is also one necessary condition for the design of individualized instruction and help for computer based systems. Individualized, user-centered, online instruction and help not only enhances knowledge acquisition processes, but is also important for the design and development of various software tools. For example, the acceptance of such tools may depend on their sensitivity to the actual knowledge and intentions of the user.

The topic of our project has been to empirically investigate and to model processes of the acquisition, utilization, and optimization of knowledge while working with the *ABSYNT Problem Solving Monitor (PSM)*. The ABSYNT PSM is designed to support the acquisition of basic functional programming concepts by supplying learners with individualized, adaptive online help and proposals. ABSYNT ("Abstract Syntax Trees") is a functional visual programming language developed in the project. The ABSYNT PSM provides help for the learner constructing ABSYNT programs to accomplish given tasks.

The design and development of a system like the ABSYNT PSM is not possible without creating models representing knowledge states and knowledge acquisition processes of learners. Our system is embedded in a *three level approach*:

♦ First, there is a theoretical framework of problem solving and knowledge acquisition: the *ISP-DL Theory* (Impasse -Success - Problem Solving - Driven Learning). Its purposes are to:

describe and explain the continuous stream of actions and verbalizations of the learner while working on programming tasks

represent a guideline for design decisions of the system

motivate and constrain models of learner's knowledge states and acquisition processes.

♦ An Internal Model or *State Model* diagnoses the actual domain knowledge of the learner (rules and schemas) at different states in the knowledge acquisition process. It is designed to be an integrated part of the ABSYNT PSM ("internal" to it) and to perform *online* knowledge

diagnosis based on computer-assessable data provided by the learner's interactions with the system. The State Model is the basis for user-adapted help.

♦ An External Model or *Process Model* is designed to simulate the knowledge acquisition processes, problem solving heuristics, and (in future) motivational processes of the learner on a level of detail not available to the State Model. The Process Model is not part of the ABSYNT PSM ("external" to it) but supports the design of the State Model. The Process Model is an *offline* model designed to bridge the gap between the ISP-DL Theory and the State Model by providing hypothetical *reasons* for the knowledge state changes represented in the State Model. For example, the Process Model should hypothesize in which kinds of situations which kinds of weak heuristics are preferred by the learner.

Thus, ISP-DL Theory, the State Model, and the Process Model are designed to be mutually consistent but serve different purposes. Figure 1 summarizes their interrelationships: The *ISP-DL Theory* controls the development of the *Process Model* and the *State Model*. Data available from the learner while working with the system are: stating and testing *hypotheses* about created solution proposals, programming actions and the time needed for them, and verbalizations. Such data are used for online construction and updating of the State Model, and/or for offline development and testing predictions of the Process Model. The State Model is in part based on an *Expert Model* representing planning knowledge and implementation knowledge of the ABSYNT domain. Both the State Model and the Expert Model are designed to provide user-adapted *help* and *explanations*.

First we will briefly describe the ISP-DL Theory since it provides the "roof" for the design of the ABSYNT PSM, the State Model, and the Process Model. Then the ABSYNT PSM is presented. In the next section we will describe the State Model and empirical analyses of some of its predictions. In addition, we show which empirical predictions follow from the State Model for different kinds of help information if the adaptivity of the information to the learner's knowledge is varied. Finally, the Process Model is described.

# The ISP-DL Theory

As indicated, the ISP-DL Theory is intended to describe the continuous stream of problem solving and learning of a student as it occurs in a sequence of, for example, programming sessions. Empirical analyses of students' sessions working with ABSYNT (Möbus & Thole, 1990; Schröder, 1990) showed that such streams can be described as an interplay of problem solving, impasse-driven learning, and success-driven learning. Several approaches have been concerned with these processes, van Lehn's theory of Impasse-Driven Learning (van Lehn, 1988, 1990, 1991b), SOAR (Laird, Newell & Rosenbloom, 1986, 1987; Newell, 1990; Rosenbloom et al., 1991); or knowledge compilation mechanisms as, for example, incorporated in ACT* (Anderson, 1983, 1986, 1989) or described by Wolff (1987, 1991). Consequently, the ISP-DL Theory is an attempt to give an integrated account of the phenomena described by these and other approaches. The ISP-DL Theory has the following features (for more detail see Möbus, 1991b; Möbus, Schröder, & Thole, in press):

◆ The distinction of different problem solving phases (according to Gollwitzer, 1990, 1991). In the *Deliberate Phase*, the problem solver (PS) thinks about several goals. A goal is a set of facts which the PS wants to become true (Newell, 1982) and can be expressed as a predicative description. This phase ends when the PS chooses one goal to pursue: The PS is now committed to an intention. In the second phase, the PS *plans* a solution for the chosen goal. A plan is a partially ordered sequence or hierarchy of subgoals which may be created by domain-specific operators or by weak heuristics. In the third phase, the plan is *executed*, and finally the result is *evaluated*. For example, the PS may check whether the obtained result satisfies the predicative description representing the main goal.

◆ *The impasse-driven acquisition of new knowledge.* Roughly, an impasse is a situation where "the architecture cannot decide what to do next given the knowledge and the situation that are at its current focus of attention." (van Lehn, 1991b, p. 19). Impasses may arise at different points in problem solving (Newell, 1990, p. 174). For example, the PS may not be able to decide on a goal, or to synthesize a plan, or a plan might not be executable, or there are no criteria to evaluate a result. In response to impasses, the PS applies weak heuristics, like asking questions, looking for help, cheating, and so on (Laird, Rosenbloom, &
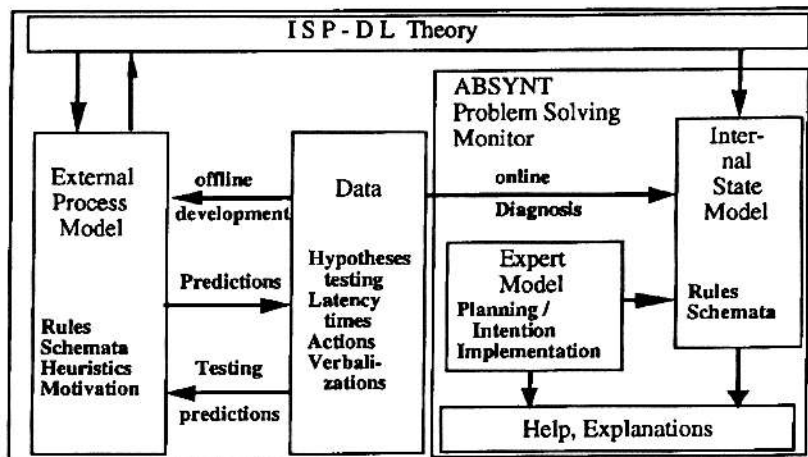
Figure 1:  The interrelationships between ISP-DL Theory, the Process Model, the State Model, the Expert Mode, the data of the learner, and help and explanations.

Newell, 1987; van Lehn, 1988, 1989, 1990, 1991b). As a result, new knowledge may be acquired that leads to overcoming the impasse. So, impasses are situations where the learner is likely to actively look for *help* (van Lehn, 1988). But it is also possible that the information obtained is not helpful. For example, information intended as help may be too complicated, or confusing, or lead in a wrong direction. So instead of solving the impasse, a secondary impasse may arise, as already described by Brown and van Lehn (1980).

♦ *The success-driven improvement of acquired knowledge.* Successfully used knowledge (knowledge which application did not lead to an impasse) may be improved so it may be used more effectively in the future. More specifically, by *rule composition* (Anderson, 1983, 1986; Lewis, 1987; Neves & Anderson, 1981; Vere, 1977) the number of control decisions and subgoals to be set may be reduced, because fewer rule selections have to be performed. In contrast to these authors, our composition is based on resolution and unfolding (Hogger,1990), see Möbus, Schröder, and Thole (1991; in press). This has theoretical and empirical advantages.

# The ABSYNT Problem Solving Monitor

ABSYNT ("Abstract Syntax Trees") is a functional, visual programming language based on ideas stated in an introductory computer science textbook (Bauer & Goos, 1982). ABSYNT is tree representation of pure LISP and is aimed at supporting the acquisition of basic functional programming skills, including abstraction and recursive systems. The design of ABSYNT as a visual programming language was based on:

◆ *two alternative executable specifications* of the ABSYNT interpreter (Möbus & Thole, 1989; Möbus & Schröder, 1990) which were developed according to cognitive science principles and constraints (Larkin & Simon, 1987; Pomerantz, 1985)

◆ empirical studies (Colonius et al., 1987; Schröder, Frank & Colonius, 1987) concerning the mental representation of and misconceptions about functional programs.

This work served to prepare the development of the ABSYNT PSM (Kohnert & Janke, 1988/91) according to principles of visual learning environments (Glinert, 1990). The motivation and analysis of ABSYNT with respect to properties of visual languages is described in Möbus and Thole (1989).

The ABSYNT PSM provides an *iconic programming environment* (Chang, 1990). Its main components are a visual *editor*, a visual *trace*, and a *help component*: a *hypotheses testing environment*. The design of the ABSYNT PSM is motivated by the ISP-DL Theory in several respects:

◆ According to the ISP-DL Theory, the learner will look for and appreciate help if he or she is caught in an impasse. Without an impasse there is no need for help. So the ABSYNT PSM does not interrupt the learner (see, for example, also Winkels & Breuker, 1990), but *offers* help. As a side effect, this design principle provides valuable data about the student's impasses.

◆ According to the ISP-DL Theory, the learner should be prevented from trapping into secondary impasses which may lead away from the original problem solving. This may be done by letting the learner make use of his pre-knowledge at impasses as much as possible. In the ABSYNT PSM, this principle is realized by the *hypotheses testing approach*. The learner may state hypotheses about which part of his current solution proposal he considers correct. The system then analyzes the hypothesis and gives feedback. The student can also ask

the system for completion proposals (see below). Another reason for the hypotheses testing approach is that in programs it is usually not possible to absolutely localize bugs. Often the bug consists of an inconsistency between program parts, and there are several ways to fix it. The hypotheses testing approach leaves the decision how to change a buggy program to the *PS*. Again, a side effect of the hypotheses testing approach is that it provides a rich data source of the learner's problem solving.

♦ According to the ISP-DL Theory, help should be provided at different levels of problem solving. The ABSYNT PSM supports the problem solving phases of *planning, executing,* and *evaluating* solution proposals. A solution proposal may be *planned* first by using goal nodes. So the learner may create a plan and test hypotheses about it without bothering about its implementation at this stage. The *implementation* of the goals (thus creating an executable program) may be done later. Finally, *evaluation* is again supported by hypothesis testing.

Figure 2 depicts snapshots from the ABSYNT PSM. Figure 2a shows the *visual editor* where ABSYNT programs can be created. There is a head window and a body window. On the left side of Figure 2a, there is the tool bar of the editor: The bucket is for deleting nodes and links. The hand is for moving, the pen for naming, and the line for connecting nodes. The "goal" node will be explained below. Next, there are constant, parameter, and "higher" operator nodes (to be named by the learner, using the pen tool). Constant and parameter nodes are the *leaves* of ABSYNT trees. Then several primitive operator nodes follow ("if", "+", "-", "*", ...). Editing is done by selecting nodes with the mouse and placing them in the windows, and by linking, moving, naming, or deleting them. Nodes and links can be created *independently*: If a link is created before the to-be-linked nodes are edited, then shadows are automatically created at the link ends. They serve as place holders for nodes to be edited later. Shadows may also be created by clicking into a free region of a window.

Constant, parameter and operator nodes are *implementation* nodes. A syntactically correct ABSYNT program is executable if it consists only of implementation nodes. Implementation nodes have three horizontal parts: an input stripe, a name stripe, and an output stripe (Constant nodes have only two stripes because name and output are identical). In the *visual trace* of the ABSYNT PSM (not depicted), input and output stripes are filled with
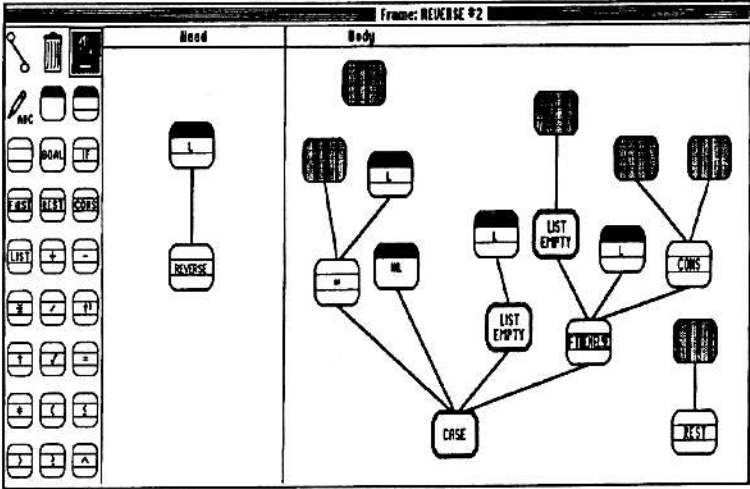
Figure 2a: Student's erroneous and overly complicated proposal in the visual editor.
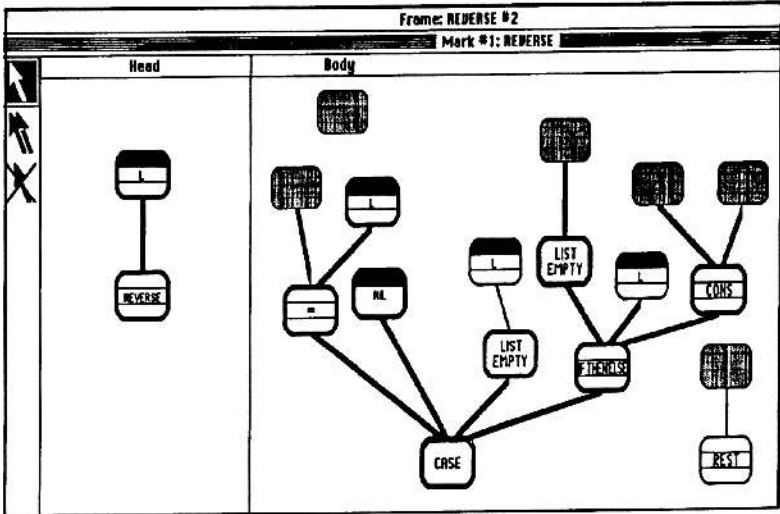


Figure 2b: Student's hypothesis (bold nodes and links).

Figure 2: Snapshots of problem solving with ABSYNT: Student's proposal to the REVERSE problem (2a), student's hypothesis proposal (2b), feedback from the ABSYNT system (2c), and the completion proposal of the ABSYNT system (2d).
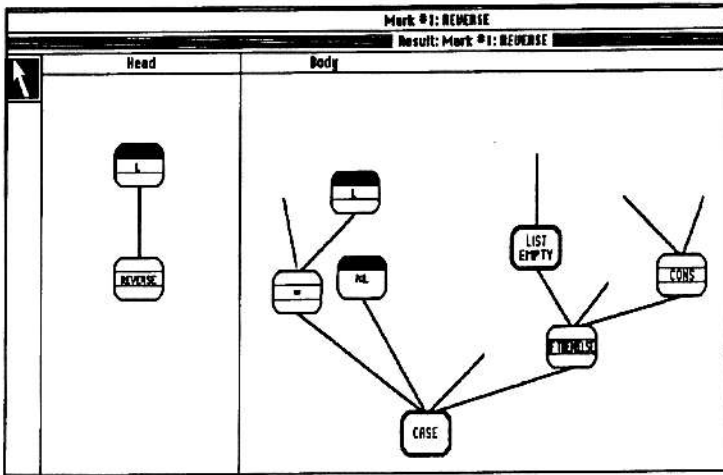
Figure 2c: Positive feedback from the ABSYNT system to the student's hypothesis

Figure 2d: Completion proposals of the ABSYNT system on student demand.

computation goals and obtained values, so each computational step of the
ABSYNT interpreter can be visualized (Möbus & Schröder, 1989, 1990;
Möbus & Thole, 1989).

But as already indicated, in ABSYNT there are also *goal* nodes designed to support *deliberating* and *planning*. Clicking on the "goal" symbol in the tool bar (Figure 2a, on the left) causes the tool bar to switch to the actual goal nodes. Goal nodes represent more abstract plan fragments which may be implemented in several ways by implementation nodes or subtrees. Visually, goal nodes have no internal structure. In Figure 2a, "LIST EMPTY" and "CASE" are examples of goal nodes. Each goal node is precisely defined as a predicative description for the yet to be implemented program fragments. For example, "LIST EMPTY" represents the goal to test whether a list is empty. The "CASE" node represents the goal to program conditionalized expressions, that is, condition-expression pairs. The ABSYNT goal nodes are based on a task analysis which applies the *transformation* approach developed in the Munich CIP Project (Bauer et al., 1987; Partsch, 1990). The transformation approach ensures that a solution can be derived to a given task that is correct with respect to the task description. Currently ABSYNT supports 42 programming tasks. For each task, there is a goal node with a predicative and a verbal task description. Data types are numbers, truth values, and lists.

In Figure 2a, a wrong solution proposal for an ABSYNT program reversing a list is just being created. There are nodes not yet linked or even completely unspecified (shaded areas). As Figure 2a shows, goal nodes and implementation nodes can be mixed ("mixed terms") within a proposal. The solution proposal in Figure 2a means:

> If L is equal to the value of a yet unknown expression,
> then the value of REVERSE is NIL,
> else if L is an empty list,
> then    if the value of a yet unknown expression is the empty list,
>         then the value of REVERSE is the value of L,
>         else the value of REVERSE is obtained by CONSing the values of two yet
>             unknown expressions together.

In the *hypotheses testing environment*, the learner may state hypotheses (bold parts of the program in Figure 2b) about the correctness of a solution proposal or parts thereof for a given programming task. The hypothesis is: "It is possible to embed the boldly marked fragment of the program in a correct solution of the current task!". The system then analyzes the hypothesis.

If the hypothesis can be confirmed the PS is shown a copy of the hypothesis (Figure 2c). If this information is not sufficient to resolve the impasse, the PS may ask for more information (completion proposals, Figure 2d). If the

hypothesis cannot be confirmed the learner receives the message that the hypothesis cannot be completed to a solution known by the system.

In Figure 2b the learner stated a hypothesis which covers a fragment of the proposal created so far for the "reverse" programming task. The hypothesis contains goal nodes and implementation nodes. The system recognizes the hypothesis as embeddable, indicating this by returning a copy of the hypothesis to the student (Figure 2c). If this information is not sufficient for solving the impasse, the student may ask the system for completion proposals at the open links.   In Figure 2d, the student asked for and received six completions (bold). Two of them are goal nodes, the others are implementation nodes. The "REVERSE" goal node represents the task goal. As far as possible, the system tries to generate completions consistent with the student's proposal. At one point, the system disagrees with the student's proposal: The system proposes "LIST NOT EMPTY" at the third input link of the CASE node, whereas the student's original proposal contains "LIST EMPTY" at this point (Figure 2a). Internally, the system has created a complete solution, but the student always gets only minimal information.

The hypotheses testing environment is the most significant aspect where the ABSYNT PSM differs from other systems designed to support the acquisition of functional programming knowledge, like the LISP tutor (Anderson & Swarecki, 1986; Anderson, Conrad, & Corbett, 1989; Corbett & Anderson, 1992), the SCENT advisor (Greer, 1992; Greer, McCalla, & Mark, 1989), and the ELM system (Weber, 1988, 1989, 1992). As indicated, one reason for the hypotheses testing approach is that in programming a bug usually cannot be absolutely localized. Hypotheses testing leaves the decision which parts of a buggy solution proposal to keep to the student and thereby provides a rich data source about the learner's knowledge and intentions. Single subject sessions with the ABSYNT PSM revealed that hypotheses testing was heavily used. It was almost the only means of debugging wrong solution proposals, despite the fact that the subjects had also the visual trace available. This is partly due to the fact that in contrast to the trace, hypotheses testing does not require a complete ABSYNT program solution. Hypotheses testing is possible with incomplete solutions, with goal nodes, and with mixed terms. So the student may obtain feedback whether he is on the right track at very early planning stages.

The answers to the learner's hypotheses are generated by rules defining a *goals-means-relation (GMR)* (Levi & Sirovich,1976; Nilsson, 1980). A subset of these rules may be viewed as "pure" expert domain knowledge not

influenced by learning. Thus, we call this set of rules EXPERT. Currently, EXPERT contains about 1300 planning rules and implementation rules. The planning rules elaborate goals and the implementation rules describe how to realize goals by ABSYNT implementation nodes.the goal decomposition done by the planning rules follows the CIP transformation approach mentioned earlier. EXPERT is able to analyze and to synthesize several millions of plans and solutions for the 42 tasks (Möbus, 1990, 1991; Möbus & Thole,1990). We think that such a large solution space is necessary because we observed that subjects, especially novices, often construct unusual solutions due to local repairs.

The completions shown in Figure 2d (bold program fragments) were generated by EXPERT rules. EXPERT analyzes and synthesizes solution proposals, but is not *adaptive* to the learner's knowledge. Usually EXPERT is able to generate a large set of *possible* completions. For example, EXPERT could generate a large number of alternatives for the "LIST NOT EMPTY" goal node in Figure 2d: for example, the goal nodes NOT, EQUAL, GREATER THAN 0 (with respect to the length of the list), or the implementation nodes =, ≠. Thus, the problem is to *select*the most appropriate completion proposal. This is the main function of the internal State Model. It represents the actual knowledge state of the learner and consists of rules derived from EXPERT. The State Model should choose a completion which is maximally *consistent* with the learner's current knowledge state. This should minimize the learner's surprise to feedback and completion proposals. The State Model is implemented, but not yet integrated into the ABSYNT PSM. It will be described in the next section.

To close this section, Figure 3 gives a summary of the components involved in planning, programming, and hypotheses testing in the ABSYNT PSM. The learner solves problems, acquires new knowledge due to impasse-driven learning, and optimizes knowledge due to success-driven learning. In Figure 3, the PS created a partial plan to the "even" task: "program that tests whether a natural number is even." The situation shows a very early stage of program development. As can be seen from the screen the PS is trying to do case analysis. His decision was to split the "even" problem into two cases. The PS defined the first case as "N EQUALS 0". Under this condition the goal "EVEN" has still to be solved. There is no proposal for the second case. The PS knows only that under the condition of the second case the original "EVEN" problem has to be solved. When the PS states a hypothesis, the system analyzes it, that is, it diagnoses the intentions (planning steps) and the
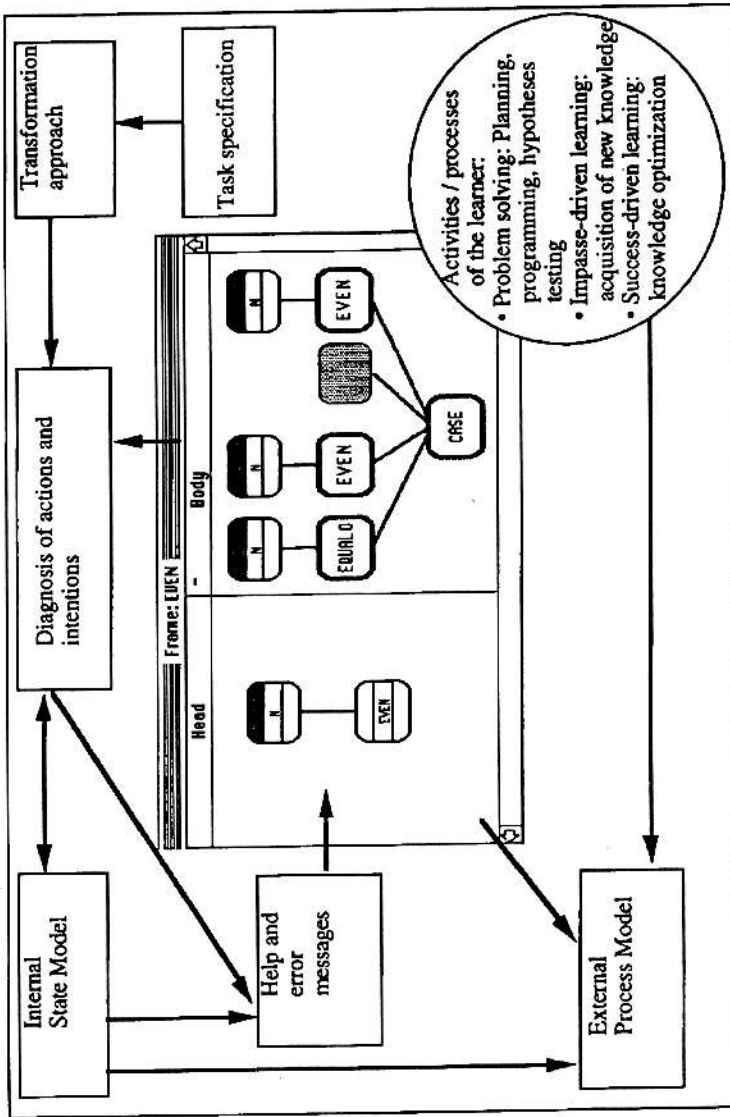
Figure 3: Planning, programming, and hypothesis testing with the ABSYNT PSM.

actions (implementation steps) of the PS. The diagnosis of actions and intentions leads to an updating of the State Model, and to positive feedback, error messages, or help (completion proposals) which are tailored to the learner. The learner will process this information (acquire new knowledge, optimize knowledge) and continue with programming, planning, or hypotheses testing. Figure 3 also shows the place of the internal process model in this framework.

## The Internal State Model

The State Model is designed as an integrated part of the ABSYNT PSM. It represents the actual hypothetical domain knowledge of the learner at different points in the knowledge acquisition process. The hypothetical domain knowledge is organized as a partial order of *micro rules, schemas*, and specific *cases*. Micro rules represent knowledge newly acquired by *impasse-driven learning* but not yet optimized. They describe small planning or implementation steps in the ABSYNT domain. Schemas and cases are created by rule composition according to the resolution method (Möbus, Schröder, Thole, in press).

The State Model is created and updated by automatically inspecting the single editing steps performed by the user while constructing ABSYNT programs (Möbus, Schröder, & Thole, 1991, in press). It is constructed according to the following, simplified description:

♦   After each programming task solved, the action trace of the PS is parsed by the micro rules, schemas, and cases of the State Model and (as far as needed) by EXPERT rules. (For example, before the learner has solved the first task, the State Model is empty, so the first solution has to be parsed completely by EXPERT rules.) According to Corbett, Anderson, and Patterson (1988) we call this process *model tracing.*

♦   The composites of all rules just used for parsing are created.

♦   Each rule used for parsing and each new composite just created is checked for *plausibility*. A rule is considered *plausible* with respect to an action trace if the ABSYNT program fragments specified by this rule are contained in the action trace in an uninterrupted temporal sequence.

◆ Each rule just found plausible is put into the State Model if it is not yet contained in it. For each plausible rule already in the state model, its credit value is raised. For composites (schemas and cases), there are two additional requirements: The part of the subject's action trace described by a composite must have been performed *earlier*, and the actual sequence has to be performed *faster* than at that earlier time. This is because composites are designed to represent knowledge optimization.

Figure 4 illustrates some of the features of the State Model. It depicts a continuous fragment of a sequence of programming actions performed by a subject. These data and associated times are stored in the action trace. To give an example, there is a micro rule in EXPERT which describes the following four actions: Placing an ABSYNT if-then-else node, and creating three input connections to it. In Figure 4, these four actions are performed at 11:15:52, 11:15:58, 11:16:46, and 11:16:55 (fragments with bold margins). So the actions corresponding to the "if-then-else-node" rule is interrupted at 11:16:42 and 11:16:50. So this rule is not plausible. This example illustrates that the State Model is created online based on detailed data: individual programming actions.

As indicated, the purpose of the State Model is to provide individualized help and completion proposals. It also gives rise to empirical predictions concerning verbalizations and order constraints on programming actions. For example, it says that as the learner shifts from novice to expert (that is, acquires successively more schemas and cases), there will not only be less verbalizations and more performance speedup, but also different order constraints for solution steps.

Figure 5 illustrates this. The upper part of Figure 5 shows a set of four micro rules, and a set of two schemas. Each rule or schema is abstractly represented as a goals-means-pair (a goal tree *g*... and an ABSYNT program fragment *a*...). The State Model postulates that if the learner applies a certain rule or schema, then the corresponding programming action(s) should be performed, and vice versa. If the learner verbalizes an intention, there should be a corresponding goal in the rule assumed to be applied. Conversely, for goals not part of the rule, there should be no verbalizations at all (middle part of Figure 5). Together with the concept of plausibility built into the State Model, this means that if the learner applies a certain rule or schema, then the corresponding action sequence of actions and goal verbalizations should be performed in an uninterrupted sequence. Actions and verbalizations stemming
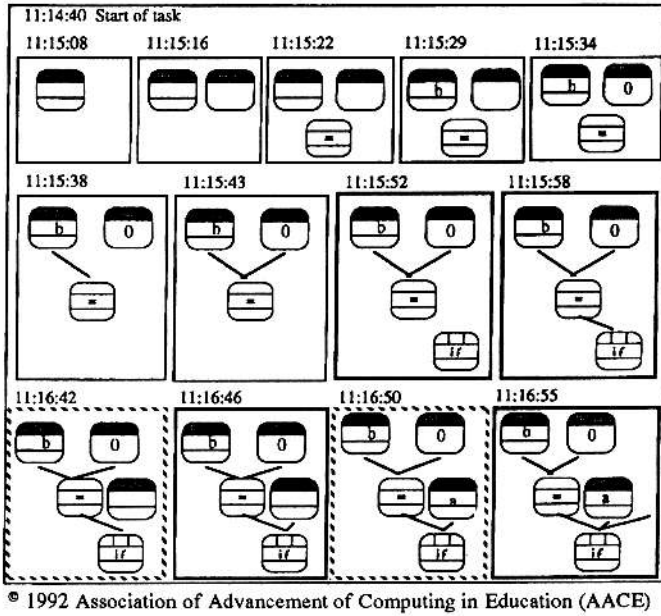
Figure 4: A continuous fragment of a sequence of programming actions performed
by a subject.

from different rules *should not interleave* (*no-interleaving hypothesis*). So if
the State Model contains the set {r1, r2, r3, r4} of micro rules, then an
empirical sequence like [g2, a1, a2, ...] should *not* be observable (Figure 5)
because a1 interrupts the sequence of events [g2, a2] explained by r2. But an
event sequence like [g2, a2, cv, a4, g4, ...] is consistent with the set {r1, r2, r3,
r4}: there is no interleaving of events explained by different rules. "cv"
denotes actions and verbalizations, like moving and rearranging nodes and
links, which are indicators of control or heuristic processes. These control
events could occur "between" events of different rules. They also should not
interrupt an event sequence explained by one rule. Control events are to be
explained by the external Process Model.

For the two schemas {s1, s2}, the prediction is that the data explained by s1
should not interleave with the data explained by s2. Again, control events
could occur "between" schema events. As Figure 5 shows, the event chain
[g2, a1, a2,...] which was inconsistent with {r1, r2, r3, r4} is *consistent* with
{s1, s2}, but an event chain like [a1, g3, g2, ...] is not, because a1 and g2 stem
from the same schema but are interrupted by g3. So *schemas lead to weaker*
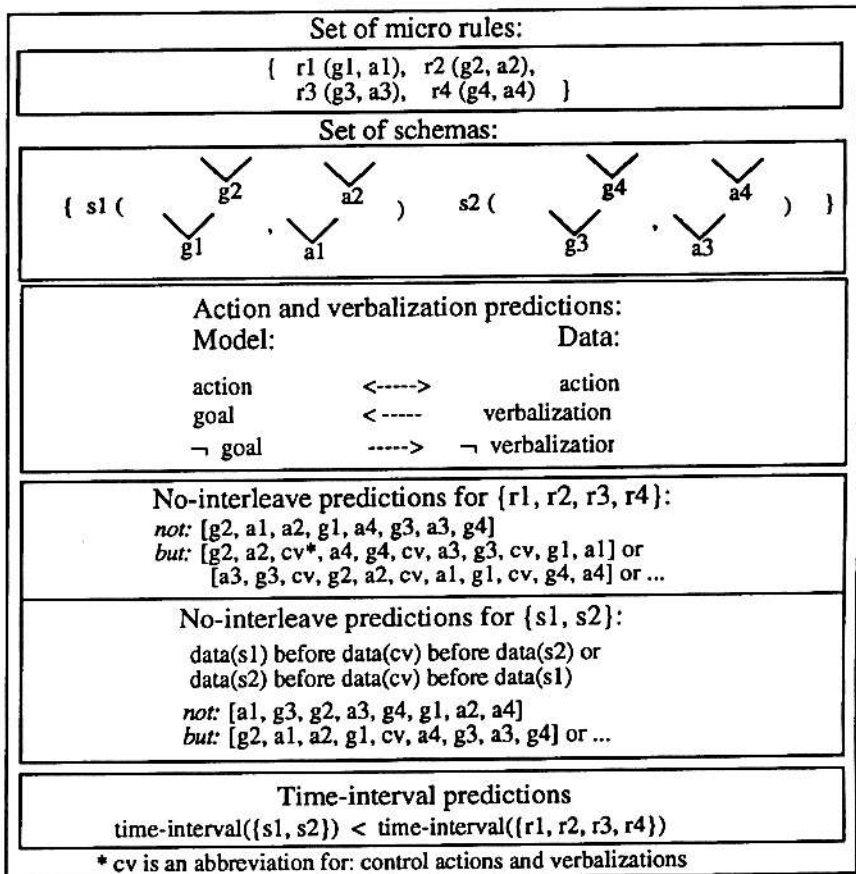
Figure 5: Empirical predictions of the State Model for micro rules vs. schemas.

*order constraints than micro rules.* But there are more predictions of the State Model: The application of the schemas should be faster than the application of the micro rules (bottom of Figure 5) because less control decisions have to be made by the learner (*time hypothesis*). For the same reason, we would expect less control actions and verbalizations, that is, less moving, repositioning, and rearranging of nodes and links (*rearrangement hypothesis*).

Some of the predictions of the State Model have been tested empirically (Möbus, Schröder, & Thole, 1992). The no-interleaving hypothesis was

investigated in the following way: The action and verbalization sequence of a single subject working with the ABSYNT PSM was videotaped and categorized, and the State Model was run offline based on the solutions created by the subject. This led to a sequence of consecutive hypothetical knowledge states of the subject. Based on this state sequence, it was predicted which actions and verbalizations of the subject should occur in uninterrupted sequences. This resulted in the *model trace* (Figure 6, on the right) which consists of sets. Each set of the model trace corresponds to the application of one State Model rule. For example, at the state depicted in Figure 6 the State Model contains a rule that describes three programming actions: to place an ABSYNT "product" node, and to draw two input links for it. So the actions and verbalizations of each model trace set are expected to occur in a continuous uninterrupted sequence. The *subject trace* (on the left of Figure 6) is the actually observed action and verbalization sequence. The subject trace was compared to the model trace in the following way: For each adjacent pair of events of the subject trace, if both events are contained in the same model trace set, then a "+" was assigned, otherwise a "-" was assigned.

For example, in Figure 6 action events 36 and 37 belong to different model trace sets, so a "-" is assigned. (On the left of the subject trace, a slightly different but equivalent method of assigning "+" and "-" is shown.) So "+" denote correspondencies of model trace and subject trace, and "-" denote contradictions. The whole subject trace contained 76 "+"and 60 "-". Since more "+" should lead to longer and thus fewer runs (continuous sequences of "+" and "-") than an equal distribution of "+" and "-", the Runs test was applied. There were 42 runs ($p < 0.001$), which is consistent with the no-interleaving hypothesis. In addition, many of the discrepancies ("-") between model trace and subject trace are due to the constant and parameter node rule (see for example events 36 and 40 in Figure 6).

How can the State Model contribute to user-adapted help generation within the ABSYNT PSM? Obviously, it should select the completion proposal to present to the learner, so the learner will receive proposals which are maximally consistent with his pre-knowledge.

But the State Model is also capable of identifying knowledge gaps - knowledge not yet acquired by the PS but necessary to continue with the actual solution proposal. Based on such a diagnosis, new empirical predictions are possible because the completion proposals selected as help by the system can be varied according to two dimensions: *grain size* and *amount*. If the grain size is *fine*, the completion proposal may rest on a chain of micro rules

| Event no. | Subject Trace | Model Trace |
|-----------|---------------|-------------|
| . | . | . |
| . | . | . |
| . | . | . |
| 36 | place constant node | { place constant node, write the value "-1" into the constant node} |
| 37 | place product node | { place product node, |
| 38 | create link from the product node to the second minus node | create link from the product node to the second minus node, |
| 39 | create link from the product node to the constant node | create link from the product node to the constant node } |
| 40 | write the value "-1" into the constant node | |
| . | . | . |
| . | . | . |
| . | . | . |

Figure 6: Empirical analysis of the State Model:  Subject trace, model trace, and
the correspondencies (+) and discrepancies (-) between them.

covering the gap.  For example, the completion proposal may consist of an
ABSYNT subtree with an explanation of the goal sequence leading to it.  If
the grain size is *coarse,* then the completion proposal may rest on a single
composite. For example, the completion proposal may consist of an ABSYNT
subtree without any explanation. Concerning *amount*, the information
provided may exactly *fill* the gap, or *too much* information is provided, or *not
enough* information so that apart of the gap remains uncovered. Different
combinations of grain size and amount lead to different hypotheses. For
example:

♦   If the information is fine-grained and exactly fills the gap, then we
     would expect that the student considers this information as *helpful.*

♦   If the information is coarse-grained and exactly fills the gap then the
     student misses explanations. So s/he might either *passively accept* what
     is being offered, or engage in *self-explanation* (van Lehn, 1991a).

◆ If the information is fine-grained but exceeds the knowledge gap, then the student has to *"filter"* the content relevant to the current situation. This might be experienced as *burdensome*.

◆ If the information leaves a small knowledge gap, then the student might try to induce one new simple rule and thereby cover the rest of the gap. (This situation seems similar to the induction of one subprocedure at a time by van Lehn's (1987) SIERRA program.)

◆ Finally, the last case to be considered here is that there is a large gap left, and the information offered is too coarse. The student should experience such an information as very inadequate to his current problem. Thus she or he should feel annoyed or even upset.

There remains much work, of course, to work out these hypotheses and put them to empirical test. But we think we have shown that the State Model is an empirically fruitful approach to knowledge diagnosis and adaptive help generation which is testable and also touches upon further research problems, like motivation and emotion.

## The External Process Model

The Process Model is aimed at modeling the knowledge acquisition *processes* which hypothetically lead to the changing knowledge states as described by the State Model. It is conceptualized as a executable realization of the ISP-DL architecture and tries to give an account of data not computer-assessable with current technology, like the learner's verbalizations.

The precursor of the Process Model was a model of the acquisition of a cognitive skill in the domain of the operational knowledge (interpreter knowledge) about ABSYNT, based on a theoretical framework of knowledge acquisition (*impasse- and success-driven learning*) which was the precursor of the ISP-DL Theory, and empirical analyses of verbal and action protocols. The starting point for this model consisted of two alternative visual rule sets based on executable specifications of the ABSYNT interpreter (Möbus & Thole, 1989). The visual rule sets were used as help material for subjects while acquiring the operational knowledge (Möbus & Schröder,1989, 1990). Rule specific hypotheses concerning memory representation and working memory load were disconfirmed (Schröder et al., 1990). Therefore, a simulation model of the knowledge acquisition process was constructed and compared to a detailed protocol of verbalizations and actions (Schröder,1990,

1992; Schröder & Kohnert, 1989/90). According to the model, new knowledge is acquired in response to impasses: Impasses trigger problem solving processes which involve the use of the help material, and existing knowledge is optimized if used successfully. The model was compared in detail to a subject trace of actions and verbalizations. It was able to hypothesize, for example, which kinds of situations lead to which kinds of weak heuristics and corresponding actions.

The external Process Model in the domain of constructing ABSYNT programs (see also Schröder & Möbus, 1992) was developed based on the ISP-DL Theory and an empirical analysis of a subject trace (actions and verbalizations) from a single subject session with ABSYNT. The analyzed part of the subject trace contained about four hours of problem solving. Figure 7 depicts the main components of the Process Model as a higher order Petri net (Huber et al., 1990). *Places* (circles /ellipses) represent states (e.g., the content of data memories, mental objects like plans or impasses, or real objects like task descriptions or solutions). *Transitions* (rectangles) represent events or process steps. The model consists of the following steps:

♦ The description of a programming task is represented as a text graph. The first step is to *understand* the task by creating a propositional task representation (Kintsch & Greeno,1985; van Dijk & Kintsch, 1983) which is a hierarchy of concept names.

♦ Based on the task representation, a *plan* for a solution proposal is created by making use of domain knowledge. The domain knowledge is a set of concepts. Each concept has a name, an input-output description that can be calculated with example values, and (possibly) an implementation in ABSYNT. So a concept corresponds to a micro rule, a schema, or a case. But a concept may be incomplete, the ABSYNT implementation may be missing. As a simple example, the concept "multiplication of two numbers" may be known, but its implementation in ABSYNT maybe unknown. (So an incomplete concept represents the pre-knowledge before working with ABSYNT.) The plan consists of instantiations of concepts of the domain knowledge.

♦ After the plan is created, there are several possibilities. The simplest possibility is that the plan is *executed*. Alternatively, an *impasse* might arise. This happens if the plan cannot be executed because of missing ABSYNT implementation knowledge in one or more concept instantiations. Now several *heuristics* are possible.
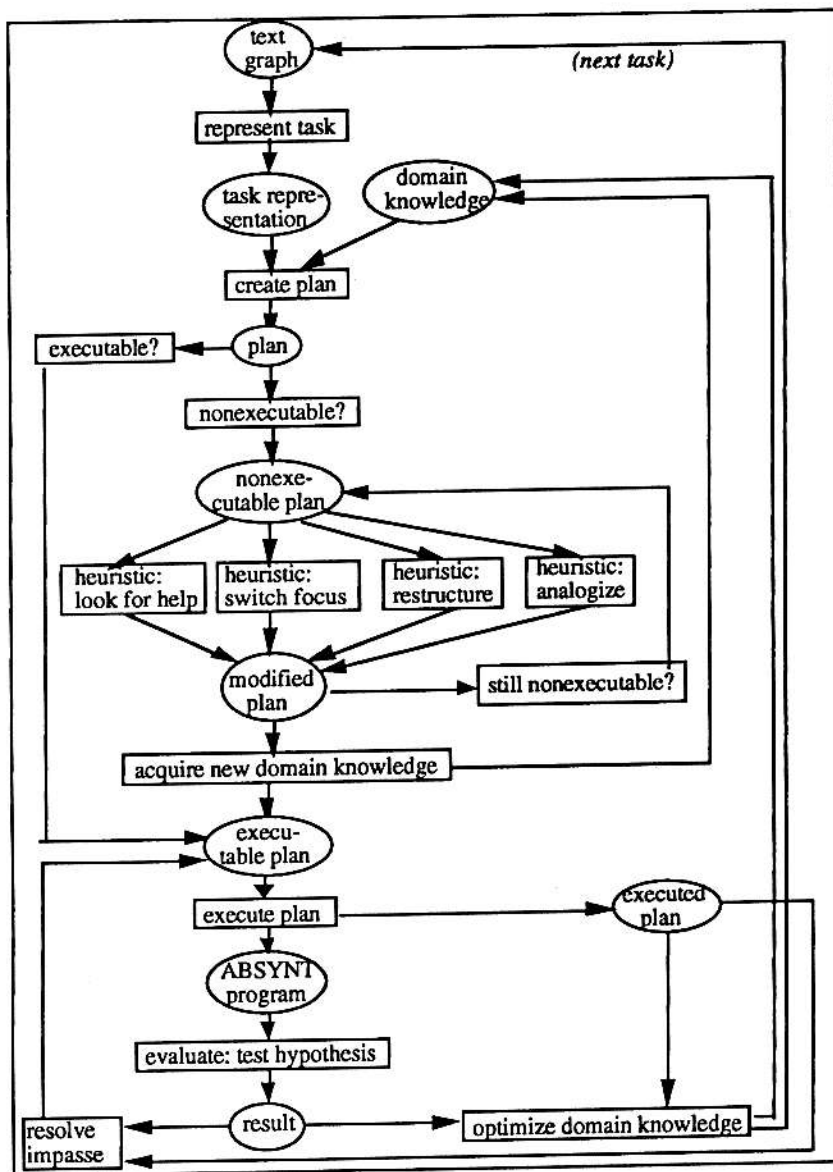
Figure 7: The external Process Model.

The first one is to look for help. The help material given to subjects consisted of example calculations of the primitive ABSYNT operator nodes. So for each primitive ABSYNT operator, the concept in question is calculated with the same input values as the example calculations. If the result is the same, then the primitive ABSYNT operator is inserted into the concept instantiation, and it is stored with the original uninstantiated concept as well (acquisition of new knowledge). If no such ABSYNT operator is found, then the heuristic has failed. Still the plan cannot be executed. The next heuristic (switch focus) is tried: Another part of the plan is implemented first. Of course this does not solve the impasse, so the impasse will be encountered again. The third heuristic is restructuring. An attempt is made to replace the concept instantiation by another one that has the same input-output behavior. (This is checked with example values). For example, the plan fragment to change the sign of a number can be replaced by multiplication with -1. If such a replacement is created, then it is stored in the knowledge base (acquisition of new knowledge), and the plan is changed accordingly. Otherwise the fourth heuristic, analogy, is tried. The analogical transfer is basically syntactical, but in addition, adjustments are made in the target solution which are again based on calculations with input-output descriptions.

♦ After an executable plan has been created and executed, the resulting ABSYNT program is *evaluated* by hypotheses testing. If the feedback is that the whole proposal is correct, then the concepts used with this task are composed, based on the executed plan, and the next task may be tried. If the feedback is that the proposal cannot be recognized by hypothesis testing, then the executed plan is debugged (= resolve impasse). Strategies of hypotheses testing and debugging are not yet part of the model.

A trace of the model was stepwise compared to the subject trace of solving five programming tasks. One result was that 65% (about 200) protocol categories of the subject trace were reproduced by the model. What is the significance of the external Process Model for the ISP-DL Theory, the internal State Model, and for help design?

♦ Concerning the *ISP-DL Theory*, the Process Model specifies types of impasses, like missing implementation knowledge and negative feedback, and hypothetical weak heuristics and the conditions for

their application. These hypotheses can be used to make the ISP-DL
Theory more detailed and empirically testable.

♦   Concerning the *State Model*, the Process Model specifies when
    which new knowledge is acquired and optimized. So the Process
    Model gives hypotheses about how the knowledge contained in the
    State Model might be generated. The Process Model might also help
    to find out how to modify the State Model if its predictions are
    disconfirmed.

♦   Concerning help design, hypotheses of the Process Model about
    weak heuristics can be used to design domain-*un*specific, "strategic"
    help. For example, with the model it should be possible to
    recommend to the learner to look for analogies in certain situations,
    or to think about reformulating goals or to ask for their preconditions
    in other situations.

## Conclusions

We described an approach to diagnose and model knowledge and knowledge
acquisition processes, and to apply these results to user-adapted help. Our
approach has three levels:

♦   a theoretical framework, the ISP-DL Theory, of problem solving and
    knowledge modification

♦   an internal State Model for online diagnosis and generation of
    user-adapted help

♦   an external Process Model for offline generation of hypotheses about
    impasses, weak heuristics, knowledge acquisition, and optimization.

The three levels are intended to be mutually consistent but serve different
purposes. The ABSYNT PSM designed to support the acquisition of basic
functional programming skills in a visual language is a concrete realization of
this approach. In line with the ISP-DL Theory, it *offers* help to the learner to
make use of at impasses, it tries to be maximally consistent with the learner's
knowledge state by hypotheses testing, and it supports the problem solving
states of planning, execution, and evaluation. Planning in ABSYNT is based
on a transformation approach. Execution leads to executable ABSYNT
programs, and evaluation is based on the hypotheses testing approach.

The internal State Model represents knowledge states consisting of newly acquired and optimized knowledge, as required by the ISP-DL Theory. It is continuously updated based on the online analysis of small action steps. It allows a large amount of predictions concerning the interleaving of action subsequences, times, and rearrangements like moving and repositioning program fragments. Some of these predictions were empirically analyzed. The external Process Model is designed to bridge the gap between the State Model and the ISP-DL Theory by providing hypothetical reasons (impasses, weak heuristics, ...) for the knowledge state changes described by the State Model.

Further work will be directed to integrate the State Model and the Process Model into the ABSYNT PSM, to investigate the empirical predictions, and to generate *explanations* of the system for positive and negative feedback in response to hypotheses testing, and to completion proposals now provided by the ABSYNT PSM.

Our three level approach has been developed in the context of functional programming, but is not constrained to it. In a related project, we develop a help system, PETRI-HELP, which is designed to support modeling concurrent or distributed processes with Petri nets (Möbus, Pitschke, & Schröder, 1992). A research goal is to study the question how much of the theory and models is domain independent.

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