

# A Greedy Knowledge Acquisition Method for the Rapid Prototyping of Knowledge Structures

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## ABSTRACT

The main goal of this paper is the presentation of a new **GR**eedy knowledge **A**cquisition **P**rocedure (GRAP) for rapid prototyping of knowledge structures (KS) or spaces. The classical knowledge acquisition method for this [2] is even for domain experts cognitive demanding and computational complex. GRAP interactively generates an online knowledge acquisition schedule so that experts only have to provide simple nonredundant judgements about the (learning / cognitive) precedence in pairs of (learning / cognitive) objects. From these data GRAP generates a Hasse diagram of the surmise relation from which the knowledge structures and optimal user-adaptive learning paths can be derived. In a case-study we developed with three expert software engineers a knowledge structure and optimal learning paths for 23 software design patterns within a few hours.

## Categories and Subject Descriptors

I.2.4 Knowledge Representation Formalisms and Methods – *representation languages, semantic networks*, I.2.6 Learning – *Knowledge Acquisition*

## General Terms

Algorithms, Measurement, Human Factors, Theory.

## Keywords

Knowledge Acquisition; Interactive Greedy Acquisition of Precedence Relations and Knowledge Structures; Interactive Greedy Construction of Transitive Closures, Hasse Diagrams and Concept Lattices;

## INTRODUCTION

Knowledge Spaces, Concept Lattices and Bayesian Belief Networks (BBN) are relevant for the success of intelligent systems in e.g. diagnostics, therapy planning, question answering and eLearning [1][2][3].

There exist only a few recommendations concerning the construction of Knowledge Spaces [2, ch.12]. Because of its cognitive demanding instructions and its runtime complexity these are unsuitable for *interactively* assessing KS

from domain experts.

This led to the development of GRAP. According to an *interactively* generated schedule controlled by GRAP experts only have to provide *simple* nonredundant judgements about the (learning / cognitive) precedence in pairs of (learning / cognitive) objects. By generating transitive closures greedily the algorithm controls the selection of nonredundant pairs, guarantees that the data comprise a partial order (*surmise relation* according to [2]) and generates the Hasse diagram of the surmise relation or the lattice of the concepts. From these structures optimal user-adaptive learning path can be derived. In the best case GRAP acquires the Hasse diagram in just one pass. In this case the savings in judgements are  $(1-2/n)*100\%$ , the judgement complexity is  $O(n)$  and the computational complexity is  $O(n^3)$ . In the worst case GRAP needs  $n(n-1)/2$  comparisons. The judgement complexity is  $O(n^2)$  and the computational complexity stays  $O(n^3)$ .

## KNOWLEDGE STRUCTURES

A KS is a pair  $(Q, K)$  of solved problems, known items, or concepts  $Q$  and a family  $K$  of subsets of  $Q$ . The subsets of  $K$  are the knowledge states in the KS. The formal definition of a KS can be found in [2]. Under the classical approach the Hasse diagram or the concept lattice has to be derived by first determining  $K$  and then the surmise relation by using the equivalence  $q_i \preceq q_j \Leftrightarrow K_i \supseteq K_j$  [2, p. 36], which can be read as: *i precedes j iff the set of knowledge states containing i is a superset of the according set containing j*. For the above mentioned reasons it is problematic to derive the precedence judgements from the set  $K$  which has to be acquired directly from experts. Instead we leave out the acquisition of  $K$  and obtain the precedence judgements  $q_i \preceq q_j$  under the control of GRAP.

## GRAP - A NEW GREEDY METHOD

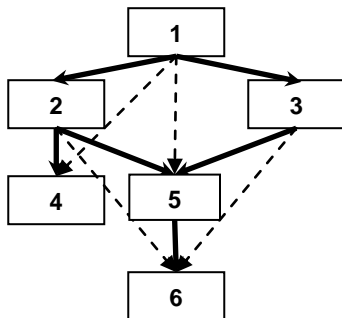
Its greediness stems from the fact that after each new data input or after each new inference all possible inferences are processed. So at any state of the knowledge acquisi-

tion process only informative new pairs are compared. After the presentation of a pair (i, j) by GRAP subjects have to select a judgement from a set of alternatives {"i causes/precedes j", "i follows j", "i neither causes/precedes nor follows j"} internally coded as {+(i, j), -(i, j), 0(i, j)}. The algorithm works parallel to the main diagonal and if it is possible to sort the items according to some vague ancestral ordering, maximizes the number of possible inferences.

**Tab 1 - GRAP controlled acquisition steps / inferences**

|   | 1  | 2              | 3              | 4              | 5               | 6              |
|---|----|----------------|----------------|----------------|-----------------|----------------|
| 1 | /  | + <sub>1</sub> | + <sub>6</sub> | ++             | ++              | ++             |
| 2 | -  | /              | 0 <sub>2</sub> | + <sub>7</sub> | + <sub>10</sub> | ++             |
| 3 | -  | 0              | /              | 0 <sub>3</sub> | + <sub>8</sub>  | ++             |
| 4 | -- | -              | 0              | /              | 0 <sub>4</sub>  | 0 <sub>9</sub> |
| 5 | -- | -              | -              | 0              | /               | + <sub>5</sub> |
| 6 | -- | --             | --             | 0              | -               | /              |

We demonstrate the algorithm with an example. First we take the KS = {∅, {1}, {1, 2}, {1, 3}, {1, 2, 3}, {1, 2, 4}, {1, 2, 3, 4}, {1, 2, 3, 5}, {1, 2, 3, 4, 5}, {1, 2, 3, 5, 6}, {1, 2, 3, 4, 5, 6}} as the "mental model" of the experts. Nodes are already numbered according a vague *ancestral ordering*. It is assumed that the experts generate judgements by comparing the set inclusion of the knowledge states according to the equivalence  $q_i \leq q_j \Leftrightarrow K_i \supseteq K_j$ . The results are shown in Table 1. Cells marked as <entry><sub><stepn></sub> are coded judgements in that order. The content of all other cells is inferred by GRAP's 13 *inference rules* (Table 2) which are triggered after any new data entrance in a cell d(i,j), and which can trigger each other *recursively*. Table 1 shows that we only need 10 judgements; the remaining 5 can be inferred by GRAP. This is a reduction of 33%. Taking only the +(i, j) order information from the transitive closure (Table 1) we are able to reconstruct the Hasse diagram (Figure 1).



**Figure 1 - Hasse diagram reconstructed from transitive closure of input data**

**Table 2 – inference rules for controlling GRAP**

| No                                     | rule   |
|--|--|
| <b>mirroring data and inferences</b>   |  |
| 1                                      | $+(i, j) \wedge \neg \neg (j, i) \Rightarrow \neg (j, i)$                    |
| 2                                      | $++(i, j) \wedge \neg \neg \neg (j, i) \Rightarrow \neg \neg (j, i)$         |
| 3                                      | $\neg (i, j) \wedge \neg + (j, i) \Rightarrow + (j, i)$                      |
| 4                                      | $\neg \neg (i, j) \wedge \neg + + (j, i) \Rightarrow + + (j, i)$             |
| 5                                      | $0(i, j) \wedge \neg 0(j, i) \Rightarrow 0(j, i)$                            |
| <b>rowwise inferences k=1,...,n</b>    |  |
| 6.1                                    | $+(i, j) \wedge + (j, k) \wedge \neg + + (i, k) \Rightarrow + + (i, k)$      |
| 7.1                                    | $+(i, j) \wedge + + (j, k) \wedge \neg + + (i, k) \Rightarrow + + (i, k)$    |
| 8.1                                    | $+ + (i, j) \wedge + (j, k) \wedge \neg + + (i, k) \Rightarrow + + (i, k)$   |
| 9.1                                    | $+ + (i, j) \wedge + + (j, k) \wedge \neg + + (i, k) \Rightarrow + + (i, k)$ |
| <b>columnwise inferences k=1,...,n</b> |  |
| 6.2                                    | $+(k, i) \wedge + (i, j) \wedge \neg + + (k, j) \Rightarrow + + (k, j)$      |
| 7.2                                    | $+(k, i) \wedge + + (i, j) \wedge \neg + + (k, j) \Rightarrow + + (k, j)$    |
| 8.2                                    | $+ + (k, i) \wedge + (i, j) \wedge \neg + + (k, j) \Rightarrow + + (k, j)$   |
| 9.2                                    | $+ + (k, i) \wedge + + (i, j) \wedge \neg + + (k, j) \Rightarrow + + (k, j)$ |

## A CASE STUDY: SOFTWARE PATTERNS

We used GRAP to find out optimized learning sequences in the domain of software design patterns. In the knowledge acquisition phase GRAP presented pairs of n=23 design patterns [4]. Experts were instructed to state whether either pattern A was a learning prerequisite for pattern B (or vice versa) or whether there was no ordering within this pair. GRAP significantly reduced the maximal number of judgements from 253 (= n(n-1)/2) to 136 (expert C), to 104 (expert B) and to 73 (expert A). So we had savings of 47% - 71%.

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