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# Further Steps towards Driver Modeling according to the Bayesian Programming Approach

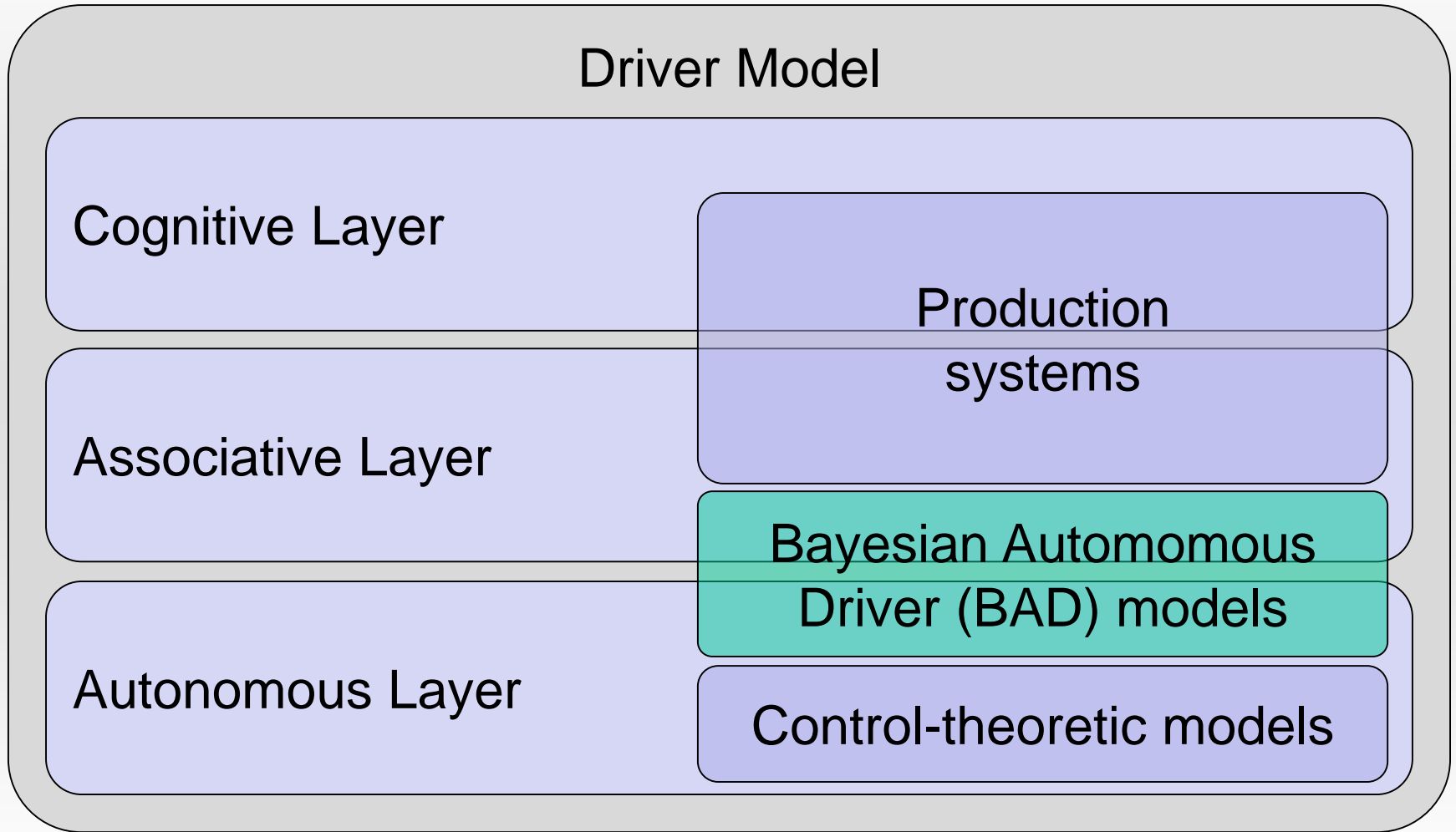
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2009/07/23

# Human driver models



# Behavior of human drivers

- The behavior of human drivers is stochastic
- The environment is stochastic

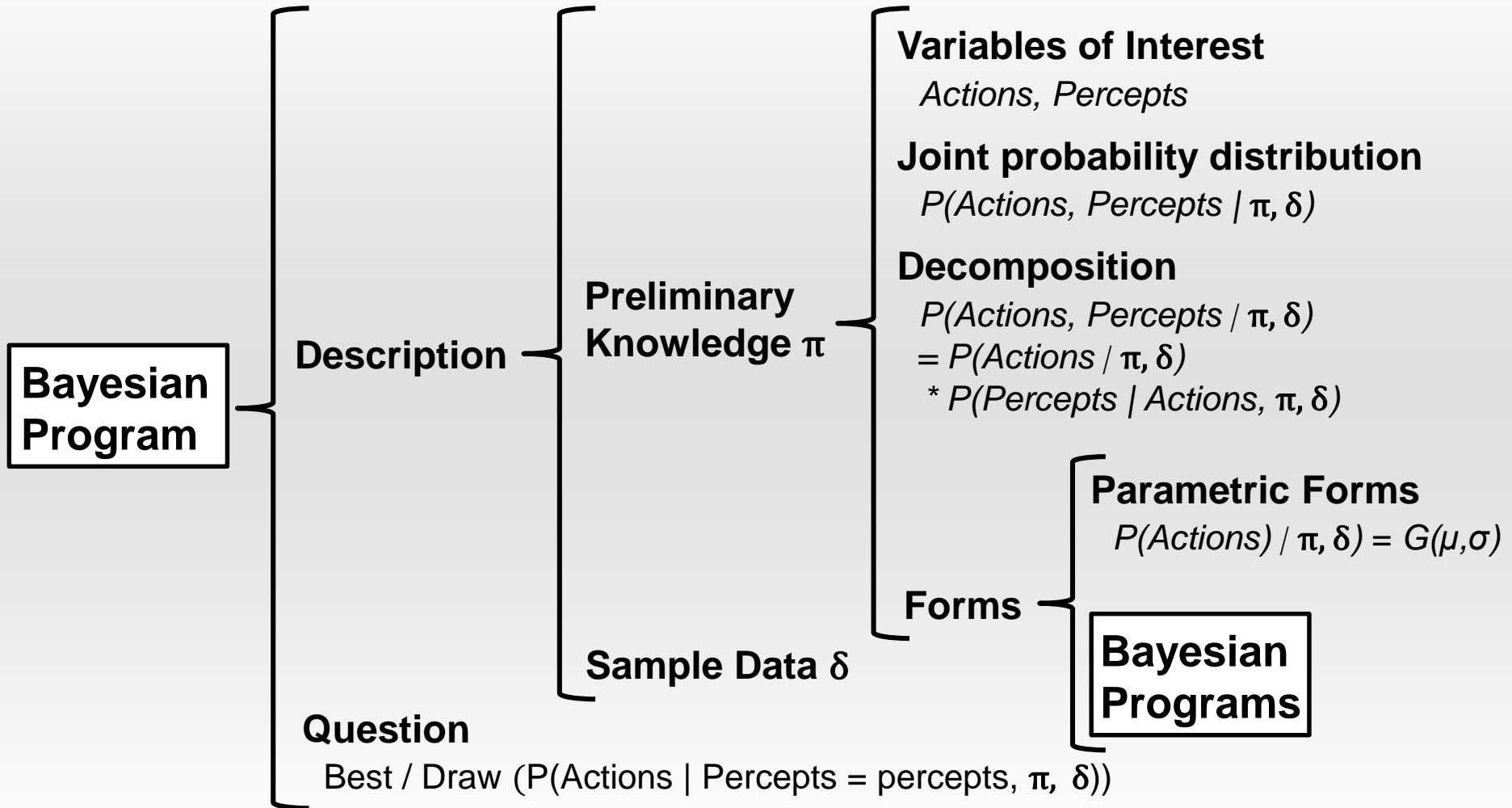


- Model human drivers with probabilistic models

# Bayesian Autonomous Driver (BAD) models

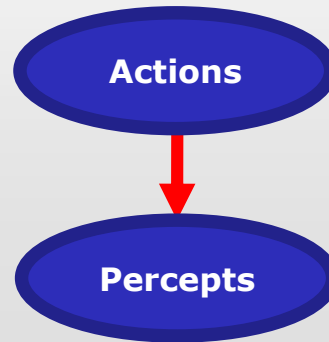
- **Valid and robust mapping from human percepts to human actions**
- **BAD models:**
  - Instances of Bayesian networks
  - Consists of a set of variables we assume to be pertinent
  - Describes relations between variables as conditional probability distributions (CPDs)
  - Infer actions under the evidence of percepts for real-time control
- **Advantages:**
  - Can be constructed with machine-learning procedures from raw sample data
  - Most assumptions testable by standard statistical methods (e.g. conditional mutual information index)

# Structure of Bayesian Programs



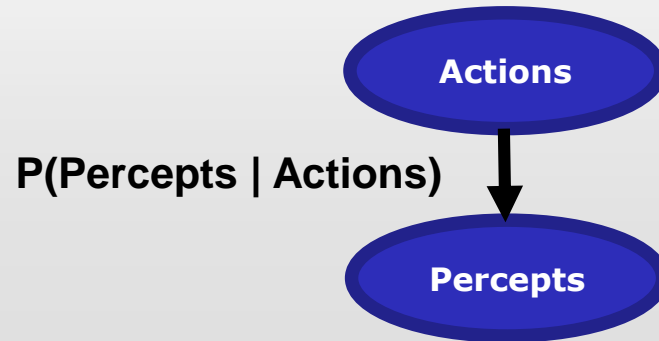
# BAD models evolving

- **First steps: Static inverse BN**



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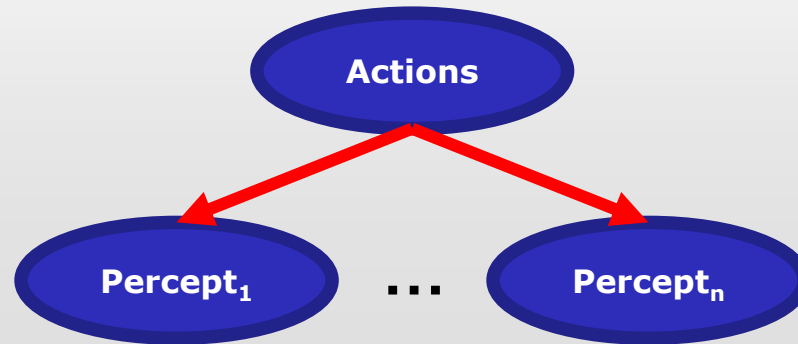
- First steps: Static inverse BN





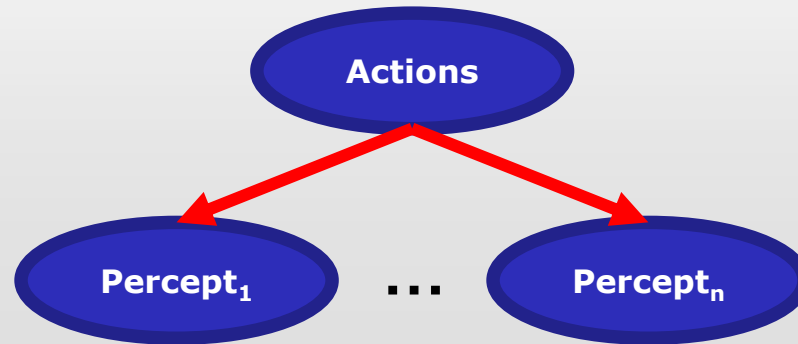
# BAD models evolving

- **First steps: Static inverse BN**
  - Sensor Fusion

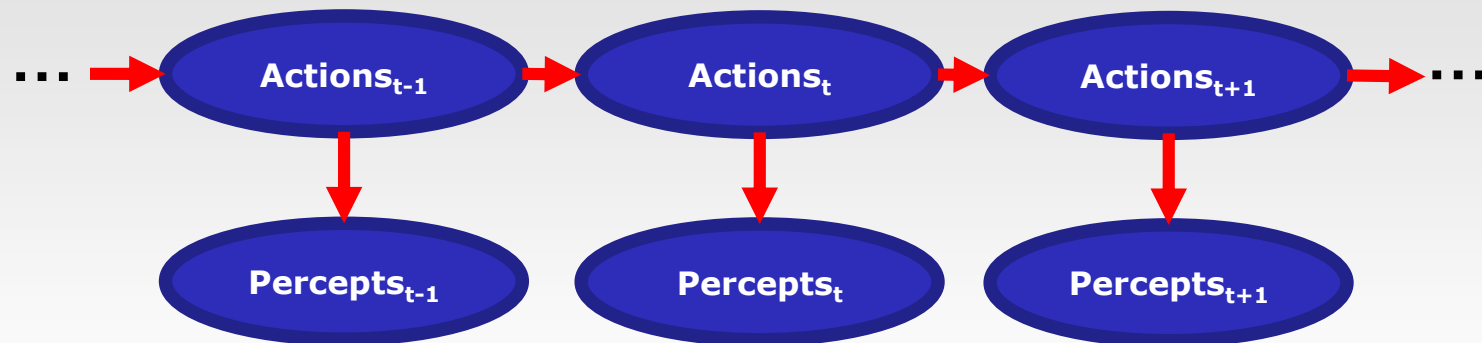


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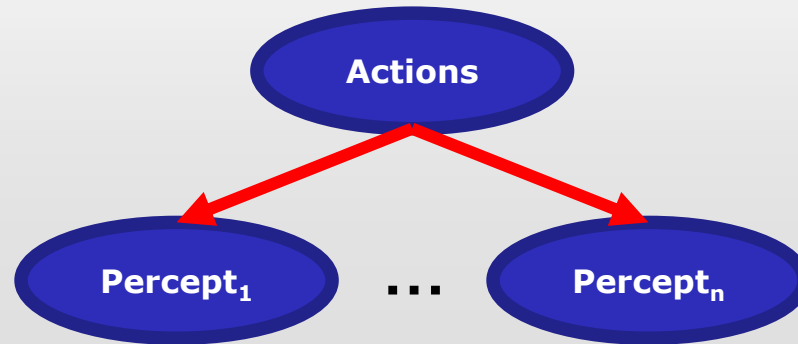


- **Further steps: Partial inverse Dynamic BN (DBN)**
  - Markov process

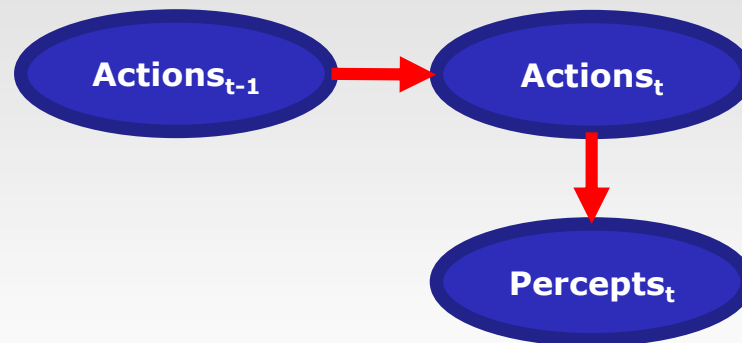


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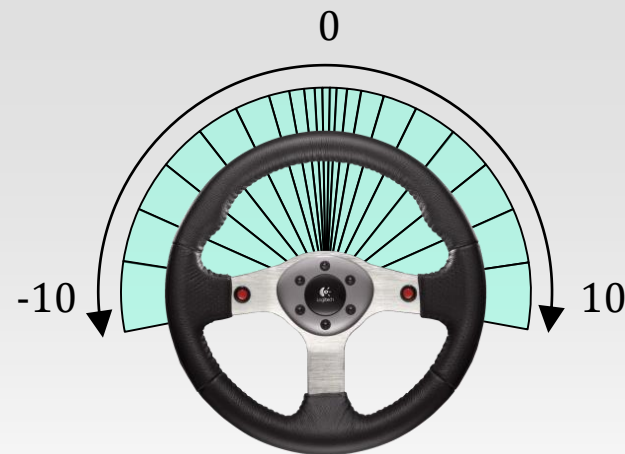
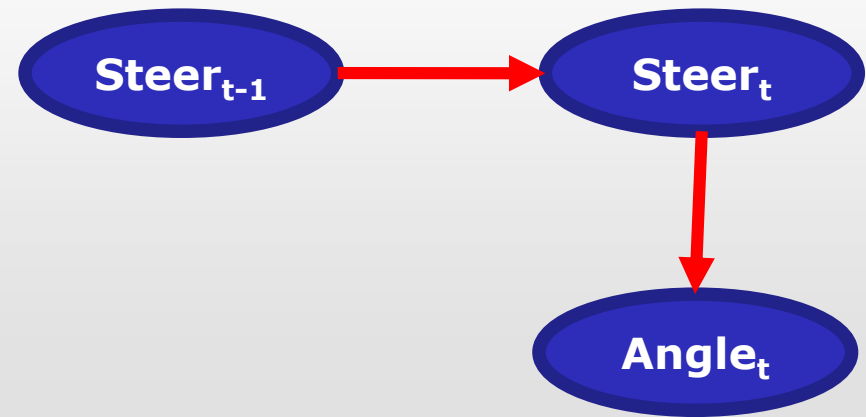


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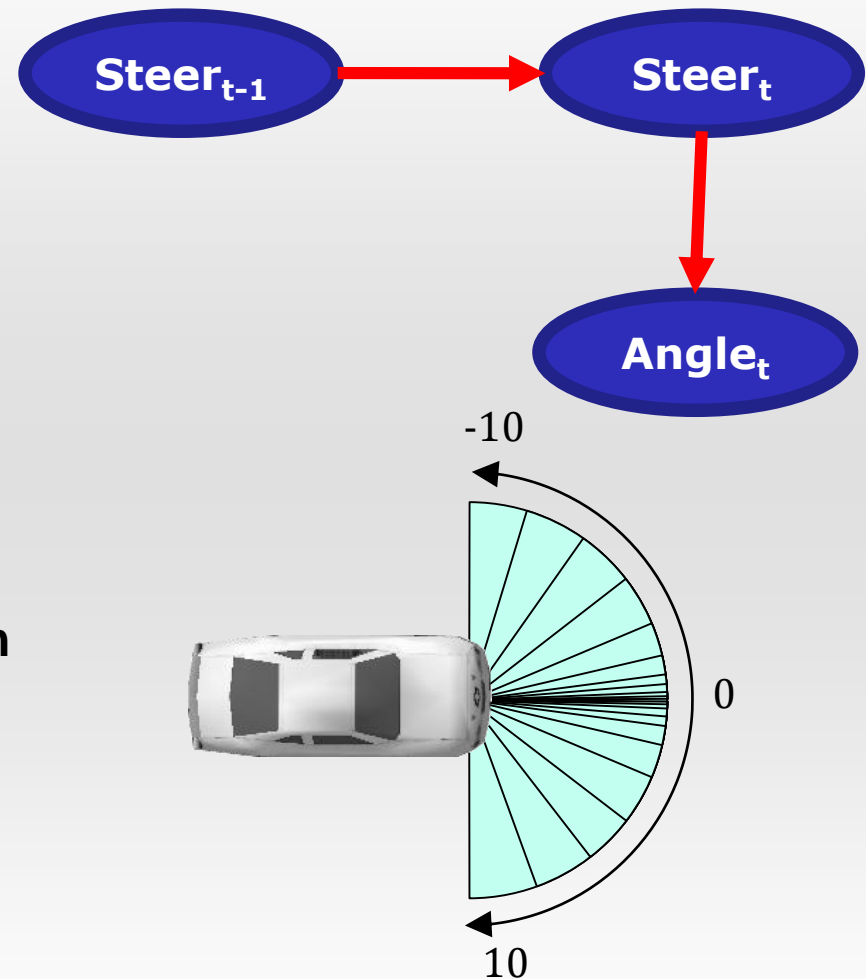
# Partial inverse DBN of lateral control

- Variables of interest:
  - $\text{Steer}_t, \text{Steer}_{t-1} \in \{-10, -9, \dots, 10\}$
  - $\text{Angle}_t \in \{-10, -9, \dots, 10\}$
  - JPD:  $P(\text{Steer}_{t-1}, \text{Steer}_t, \text{Angle}_t)$
- Decomposition of JPD:
  - $P(\text{Steer}_{t-1}, \text{Steer}_t, \text{Angle}_t)$   
=  $P(\text{Steer}_{t-1}) * P(\text{Steer}_t | \text{Steer}_{t-1})$   
\*  $P(\text{Angle}_t | \text{Steer}_t)$
- Parameters will be derived from time series of variables
- Question:
  - $\text{Draw}(P(\text{Steer}_t | \text{steer}_{t-1}, \text{angle}_t))$



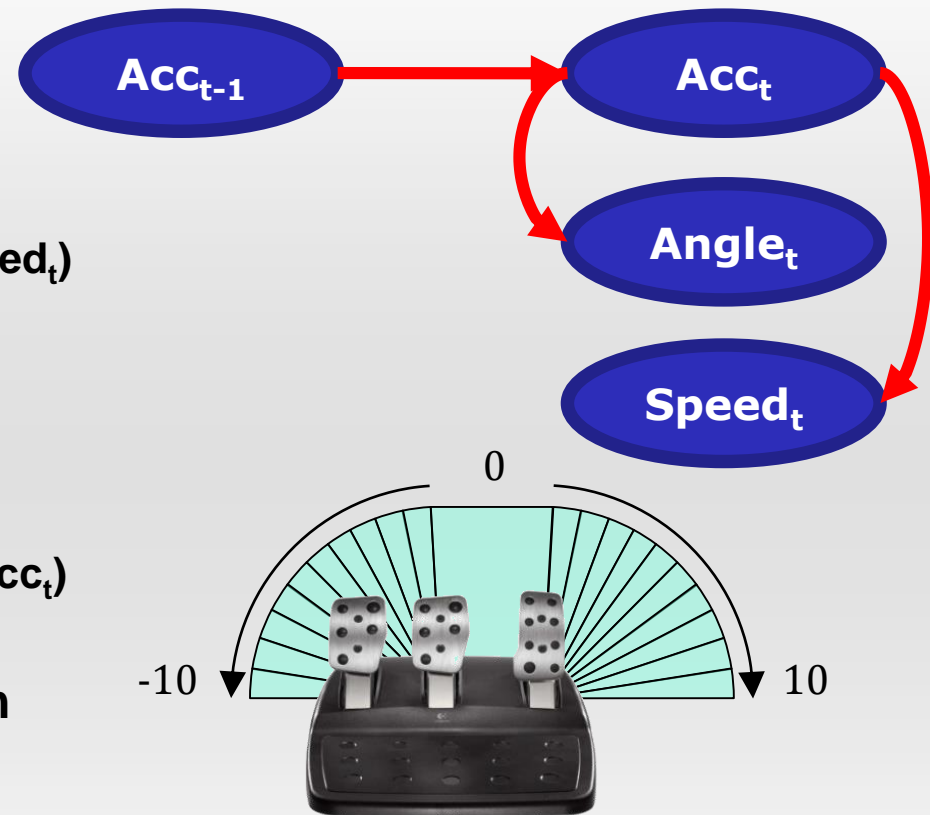
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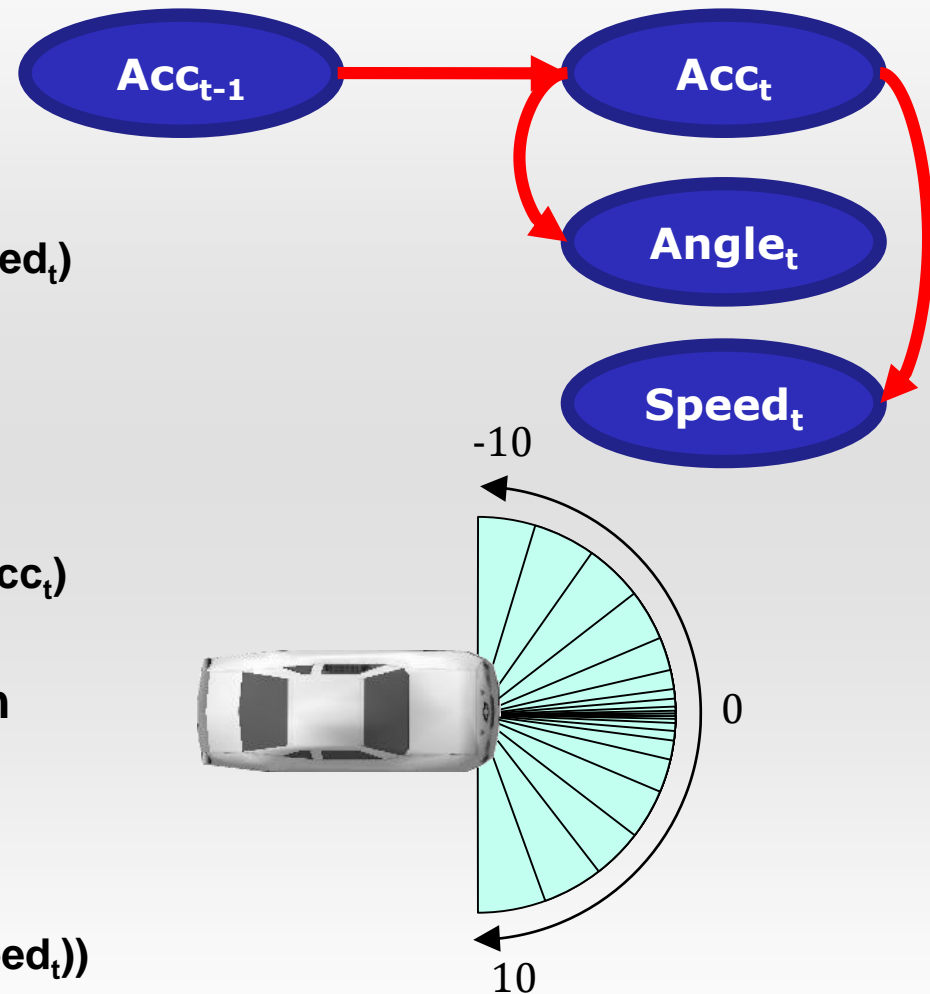
# Partial inverse DBN of longitudinal control

- Variables of interest:
  - $Acc_{t-1}, Acc_t \in \{-10, -9, \dots, 10\}$
  - $Angle_t \in \{-10, -9, \dots, 10\}$
  - $Speed_t \in \{0, 1, \dots, 9\}$
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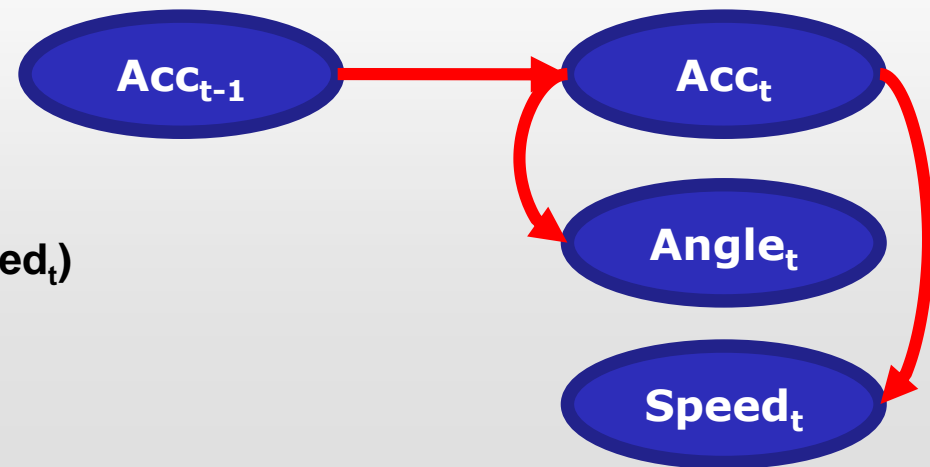
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# Partial inverse DBN of longitudinal control

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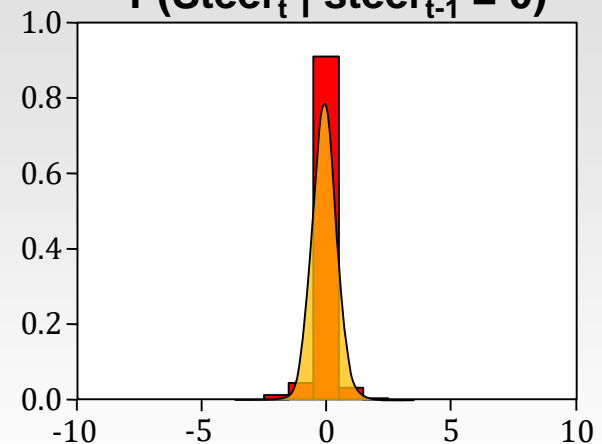


# Experimental setting

- **TORCS racing simulation**
  - Racing track „Aalborg“
- **ProBT API and inference engine**
- **Recorded time series of variables during manually driving one single lap**
  - $\Delta t = 50$  ms
- **Deriving conditional histograms from time series for each conditional probability distribution**
- **Discretized histograms by mean and standard deviation when plausible**



$P(\text{Steer}_t \mid \text{steer}_{t-1} = 0)$

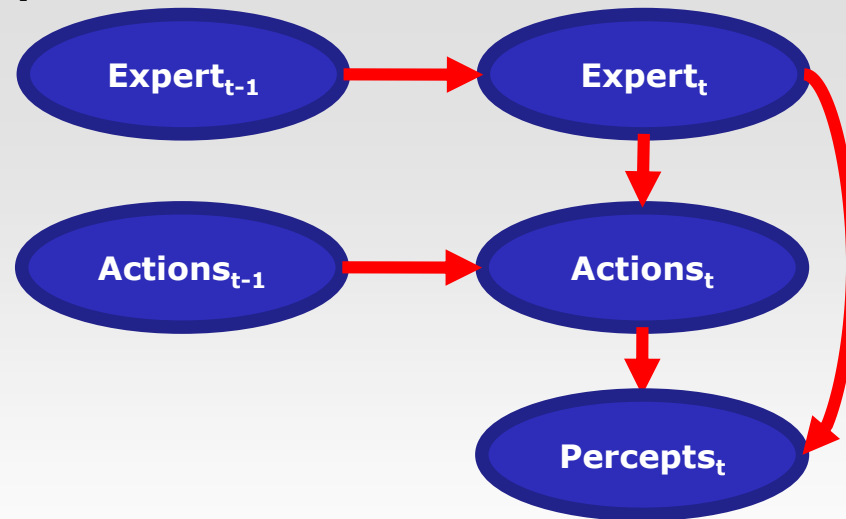


# BAD model performance in TORCS



# Steps beyond...

- **Mixture of Experts BAD model**
  - Experts make related actions and percepts more probable
  - Context dependent driver behavior by mixing pure behavior from different experts
  - Learn new skills without forgetting already learnt ones
  - Avoid the stability-plasticity dilemma
- **Combine models of lateral / longitudinal control**
- **Improve perception**



Thank You for Your Attention